If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet. Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen. You may use an HB pencil for any diagrams or graphs. Do not use staples, paper clips, glue or correction fluid. DO NOT WRITE IN ANY BARCODES.

Answer all the questions. Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question. The use of an electronic calculator is expected, where appropriate. You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [ ] at the end of each question or part question. The total number of marks for this paper is 75. Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.
1 Solve the inequality $2|x - 2| > |3x + 1|$. [4]

2 The variables $x$ and $y$ satisfy the relation $3^y = 4^{2-x}$.
   
   (i) By taking logarithms, show that the graph of $y$ against $x$ is a straight line. State the exact value of the gradient of this line. [3]
   
   (ii) Calculate the exact $x$-coordinate of the point of intersection of this line with the line with equation $y = 2x$, simplifying your answer. [2]

3 (i) Express $(\sqrt{5}) \cos x + 2 \sin x$ in the form $R \cos(x - \alpha)$, where $R > 0$ and $0^\circ < \alpha < 90^\circ$, giving the value of $\alpha$ correct to 2 decimal places. [3]
   
   (ii) Hence solve the equation
   
   $$(\sqrt{5}) \cos \frac{1}{2}x + 2 \sin \frac{1}{2}x = 1.2,$$
   
   for $0^\circ < x < 360^\circ$. [3]

4 The parametric equations of a curve are
   
   $$x = t + \cos t, \quad y = \ln(1 + \sin t),$$
   
   where $-\frac{1}{2}\pi < t < \frac{1}{2}\pi$.
   
   (i) Show that $\frac{dy}{dx} = \sec t$. [5]
   
   (ii) Hence find the $x$-coordinates of the points on the curve at which the gradient is equal to 3. Give your answers correct to 3 significant figures. [3]

5 The variables $x$ and $y$ satisfy the differential equation
   
   $$\frac{dy}{dx} = e^{-2y} \tan^2 x,$$
   
   for $0 \leq x < \frac{1}{2}\pi$, and it is given that $y = 0$ when $x = 0$. Solve the differential equation and calculate the value of $y$ when $x = \frac{1}{4}\pi$. [8]

6 The curve with equation $y = x^2 \cos \frac{1}{2}x$ has a stationary point at $x = p$ in the interval $0 < x < \pi$.
   
   (i) Show that $p$ satisfies the equation $\tan \frac{1}{2}p = \frac{4}{p}$. [3]
   
   (ii) Verify by calculation that $p$ lies between 2 and 2.5. [2]
   
   (iii) Use the iterative formula $p_{n+1} = 2 \tan^{-1}\left(\frac{4}{p_n}\right)$ to determine the value of $p$ correct to 2 decimal places. Give the result of each iteration to 4 decimal places. [3]
7. Let \( I = \int_0^1 \frac{x^5}{(1 + x^2)^3} \, dx \).

(i) Using the substitution \( u = 1 + x^2 \), show that \( I = \int_1^2 \frac{(u - 1)^2}{2u^2} \, du \). [3]

(ii) Hence find the exact value of \( I \). [5]

8. The points \( A \) and \( B \) have position vectors, relative to the origin \( O \), given by \( \overrightarrow{OA} = \text{i} + \text{j} + \text{k} \) and \( \overrightarrow{OB} = 2\text{i} + 3\text{k} \). The line \( l \) has vector equation \( r = 2\text{i} - 2\text{j} - \text{k} + \mu(-\text{i} + 2\text{j} + \text{k}) \).

(i) Show that the line passing through \( A \) and \( B \) does not intersect \( l \). [4]

(ii) Show that the length of the perpendicular from \( A \) to \( l \) is \( \frac{1}{\sqrt{2}} \). [5]

9. Throughout this question the use of a calculator is not permitted.

The complex numbers \(-1 + 3\text{i} \) and \( 2 - \text{i} \) are denoted by \( u \) and \( v \) respectively. In an Argand diagram with origin \( O \), the points \( A, B \) and \( C \) represent the numbers \( u, v \) and \( u + v \) respectively.

(i) Sketch this diagram and state fully the geometrical relationship between \( OB \) and \( AC \). [4]

(ii) Find, in the form \( x + iy \), where \( x \) and \( y \) are real, the complex number \( \frac{u}{v} \). [3]

(iii) Prove that angle \( AOB = \frac{3\pi}{4} \). [2]

10. Let \( f(x) = \frac{10x - 2x^2}{(x + 3)(x - 1)^2} \).

(i) Express \( f(x) \) in partial fractions. [5]

(ii) Hence obtain the expansion of \( f(x) \) in ascending powers of \( x \), up to and including the term in \( x^2 \). [5]